



Two-Phase Flow



L.K.H. Leung
Thermalhydraulics Branch
Chalk River Laboratories, AECL

UNENE Thermalhydraulics Course

Canada 



AECL
Atomic Energy
of Canada Limited

EACL
Énergie atomique
du Canada limitée



Outline

- **Introduction**
- **Terminologies**
- **Model assumptions**
- **Flow patterns**
- **Boiling flow**
- **Void fraction**
- **Summary**



Background

- **Two-phase flow is encountered in many engineering systems of chemical, process, power generation, and petroleum industries**
- **Typical examples are oil-gas pipelines, boilers, heat exchangers, refrigeration equipment, evaporators, nuclear reactors, etc.**
- **In a simple way, two-phase flow is an extension of single-phase flow**
- **In reality, two-phase flow is much more complex due to the uncertainty in various interfacial parameters**
- **Correlations are often applied in design calculations**

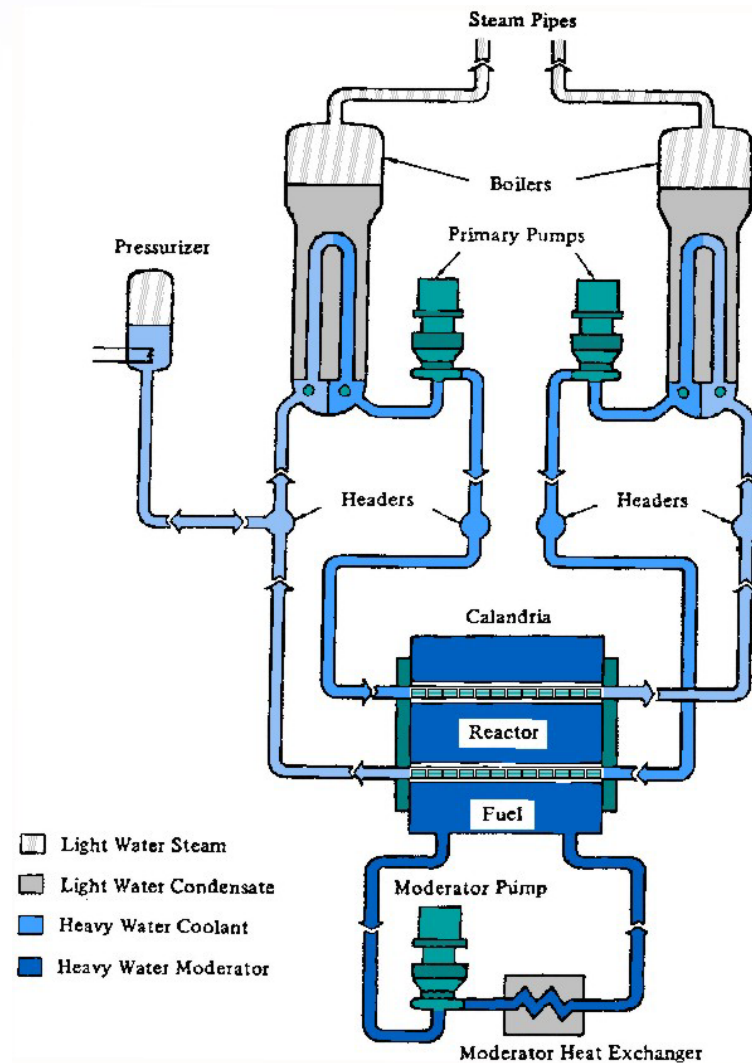


Terminologies

- **Two-phase flow**
 - Simultaneous flow of liquid and vapour of a single substance
 - Examples: reactor fuel channels, steam generators, kettle on a hot stove
 - Also referred to as “Single-component two-phase flow”
- **Two-component flow**
 - Simultaneous flow of liquid and gas of two substances
 - Examples: oil-gas pipelines, beer, soft drink
 - Also referred to as “Two-component two-phase flow”



Two-Phase Flow in Primary HTS





Analytical Parameters

- **Primary parameters**
 - Thermal: power
 - Hydraulics: pressure, mass flow rate, fluid temperature, pressure drop
 - Geometry: flow and heated areas, hydraulic and heated equivalent diameters
- **Calculated parameters commonly used in analyses**
 - Mass flux, heat flux
 - Quality: mass, equilibrium, thermodynamic
 - Void fraction
- **Fluid properties**
 - Density, viscosity, enthalpy, thermal conductivity, heat capacity



Key Definitions

- **Void fraction is ratio of area occupied by vapour/gaseous phase to total flow area**

$$\alpha = \frac{A_g}{A}; \quad (1 - \alpha) = \frac{A_f}{A}$$

- **Mass quality is ratio of vapour mass flow to total mass flow**

$$x = \frac{W_g}{W} = \frac{W_g}{W_f + W_g}; \quad (1 - x) = \frac{W_f}{W} = \frac{W_f}{W_f + W_g}$$

- **Mass flux is mass flow rate per unit flow area**

$$G = \frac{W}{A} = \rho u = \frac{u}{v}; \quad G_g = G x; \quad G_f = G (1 - x)$$

- **Volumetric flux (or superficial velocity) is volumetric flow rate over the total flow area**

$$j = \frac{Q}{A}; \quad j_g = \frac{Q_g}{A}; \quad j_f = \frac{Q_f}{A}$$



Phasic Velocity Definitions

- **Vapour phase velocity**

$$u_g = \frac{W_g}{\rho_g A_g} = \frac{Q_g}{A_g} = \frac{G x}{\rho_g \alpha}$$

- **Liquid phase velocity**

$$u_f = \frac{W_f}{\rho_f A_f} = \frac{Q_f}{A_f} = \frac{G (1-x)}{\rho_f (1-\alpha)}$$

- **Slip ratio = (vapour velocity)/(liquid velocity)**

$$\frac{u_g}{u_f} = \frac{W_g \rho_f A_f}{W_f \rho_g A_g} = \left(\frac{x}{1-x} \right) \left(\frac{\rho_f}{\rho_g} \right) \left(\frac{1-\alpha}{\alpha} \right)$$



Quality Definitions

- **Mass quality**

- Direct measurements of vapour and liquid flow
- Varies from 0 to 100%

$$x = \frac{W_g}{W} = \frac{W_g}{W_f + W_g}$$

- **Thermodynamic quality**

- Based on enthalpy balance
- Varies from negative to positive values greater than 100%

$$x = \frac{h - h_f}{h_{fg}}$$

- **Equilibrium quality**

- Thermodynamic quality at equilibrium conditions
- Same as mass quality (varies from 0 to 100%)



Model Assumptions

- **Homogeneous flow model**
 - The two-phase flow is assumed to behave as a single-phase flow with mean fluid properties
 - Equal vapour and liquid velocities
 - Thermodynamic equilibrium between these phases
- **Separated flow model**
 - The two phases are considered separate with different fluid properties
 - Constant but not necessarily equal velocities for the two phases
 - Thermodynamic equilibrium between these phases
- **Flow-regime dependent model**
 - Between homogeneous flow and separated flow assumptions
 - Complex
 - Requires good flow-pattern transition criterion



Flow Patterns

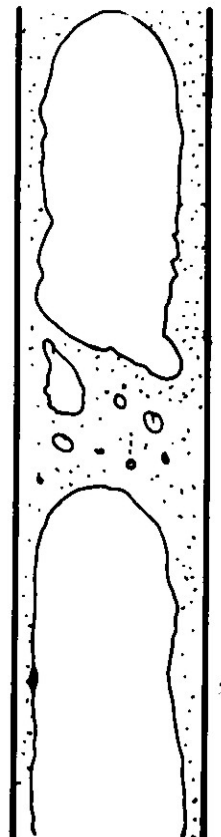
- **Distribution of phases inside a confined area**
- **Depend strongly on liquid and vapour velocities**
- **Channel geometry**
 - Minor effect for simple channel with no interconnected subchannel
 - Complex for channel with interconnected subchannel (such as bundle) due to flow and quality distributions
- **Surface heating**
 - Influence near-wall flow patterns resulted in an internal void gradient
 - Wrap-around dry-wall flow patterns not encountered in adiabatic conditions
- **Appendages**
 - Homogenize the flow pattern at downstream locations
 - Transit back to basic pattern at locations far away



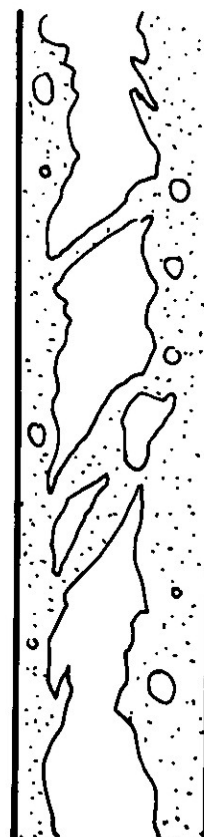
Flow Patterns in Vertical Flow



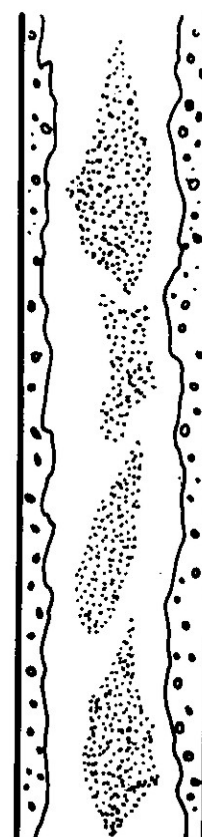
Bubbly



Slug



Churn



Wispy-annular



Annular



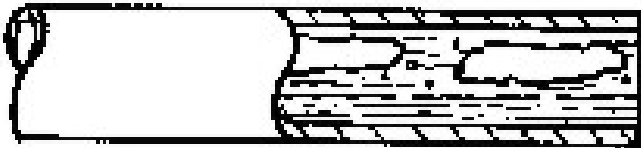
Flow Patterns in Horizontal Flow



Bubbly



Wavy



Plug



Slug



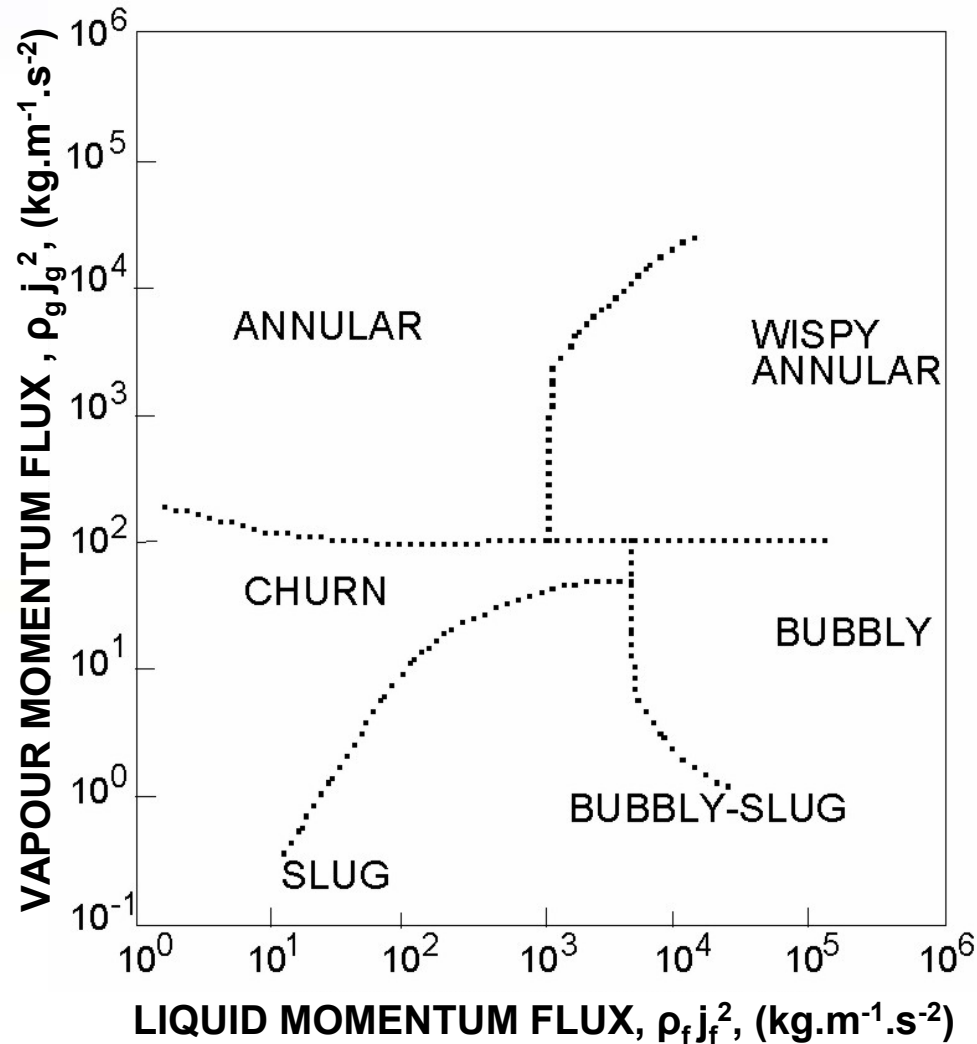
Stratified



Annular

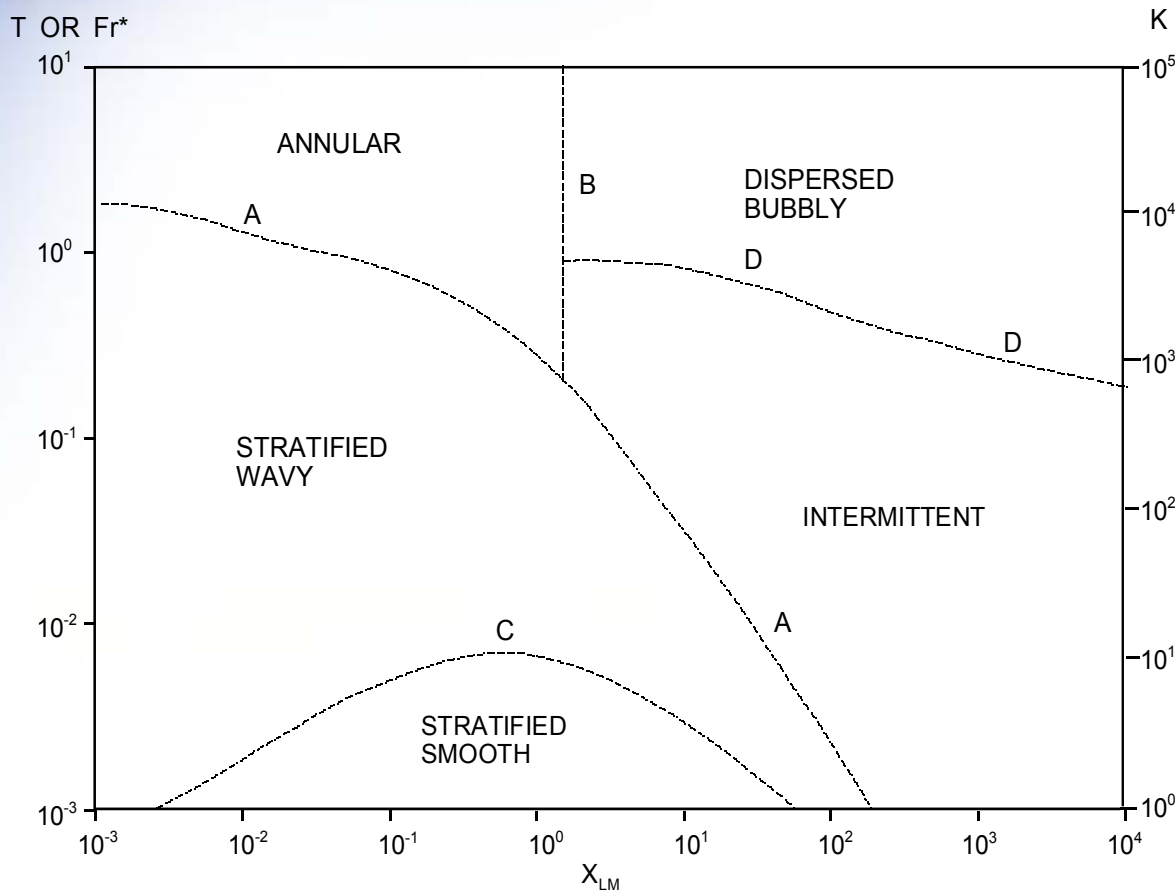


Flow Pattern Map for Vertical Flow





Flow Pattern Map for Horizontal Flow



CURVES : A & B C D
 COORDINATES : Fr^* vs. X_{LM} K vs. X_{LM} T vs. X_{LM}

$$X_{LM} = \left(\frac{(dP/dZ)_{f, \text{fric.}}}{(dP/dZ)_{g, \text{fric.}}} \right)^2$$

$$Fr^* = \left(\frac{\rho_g}{\rho_f - \rho_g} \right)^{0.5} \frac{j_g}{(D g \cos \theta)^{0.5}}$$

$$K = \left(\frac{\rho_g j_g^2 j_f}{(\rho_f - \rho_g) g v_f \cos \theta} \right)^{0.5}$$

$$T = \left(\frac{(dP/dz)_{f, \text{fric.}}}{(\rho_f - \rho_g) g \cos \theta} \right)^{0.5}$$

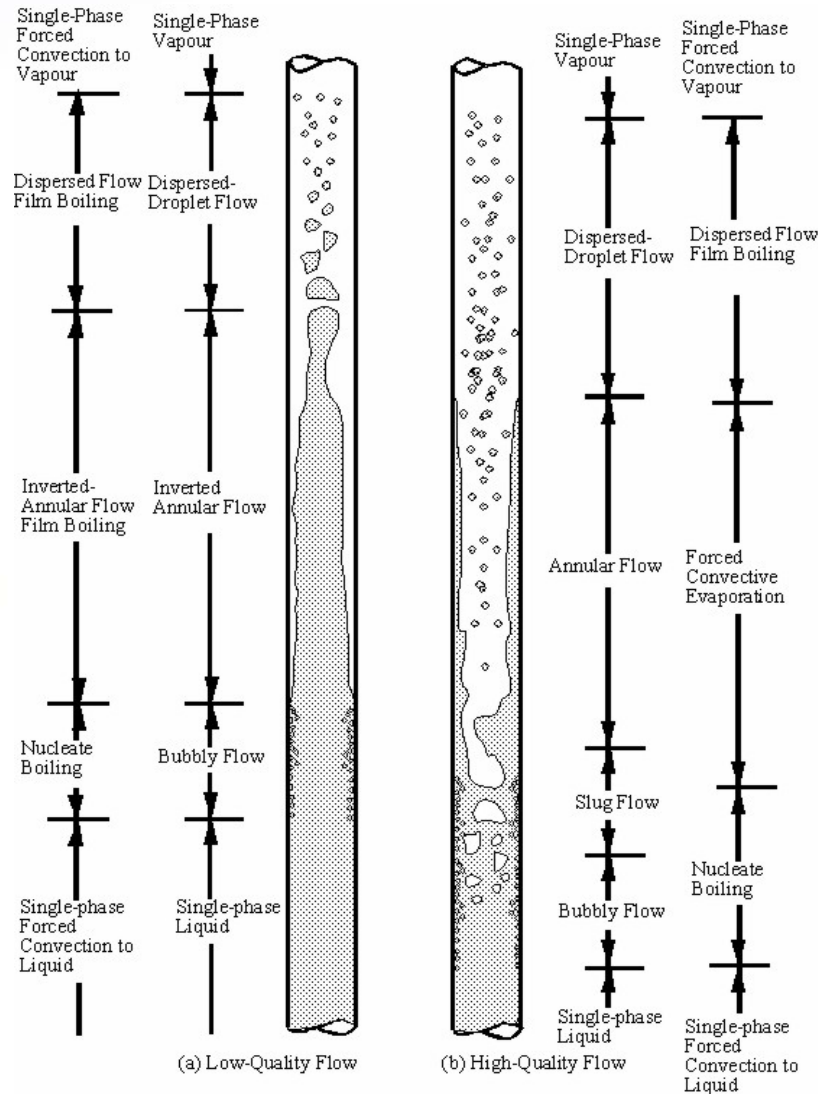


Boiling

- **Vapour formation (nucleation)**
 - Liquid superheating (at the surface)
 - Homogeneous (molecular dynamic within the fluid)
 - Heterogeneous (requires nucleation sites in the fluid or at the surface)
- **Bubble detachment**
 - Balance of dynamic, buoyancy and surface tension forces
- **Types**
 - Pool boiling
 - Convective boiling

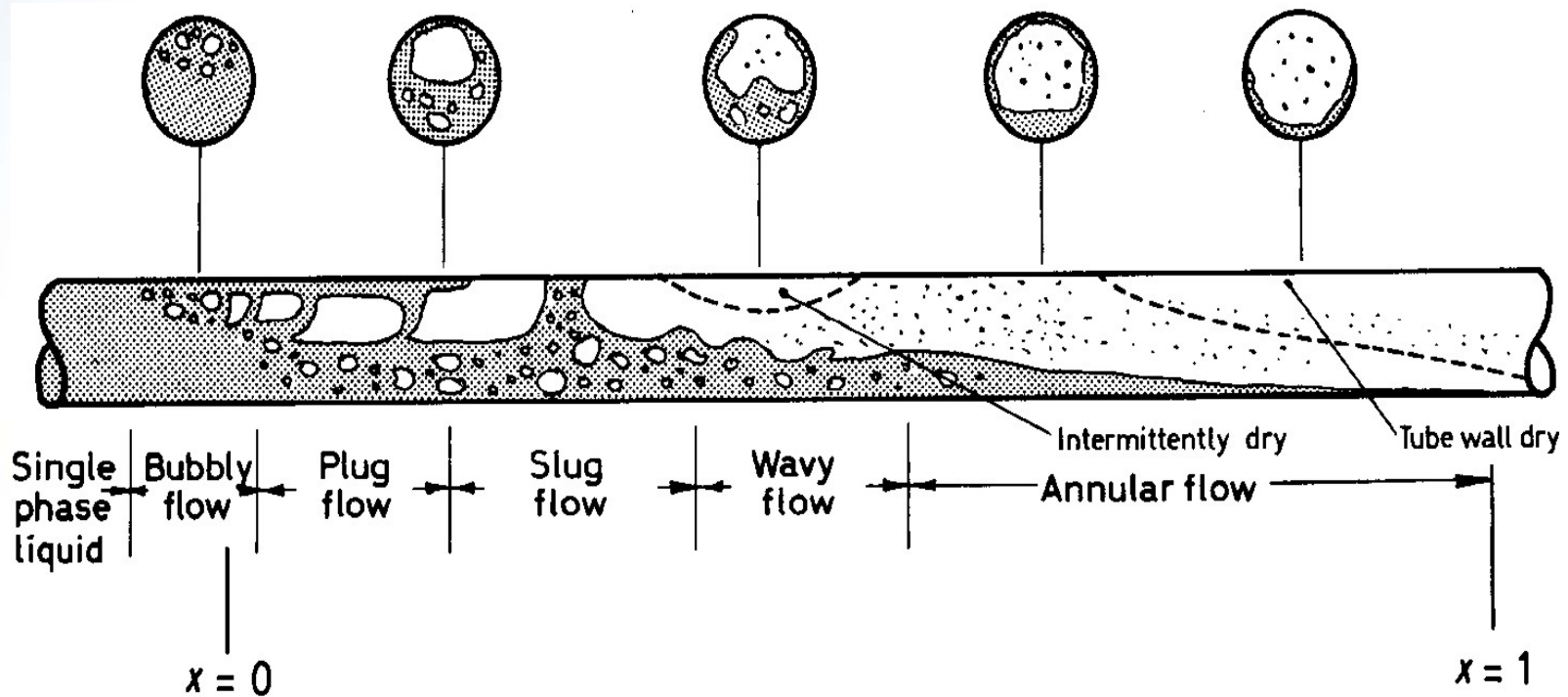


Flow Patterns in Vertical Heated Channels



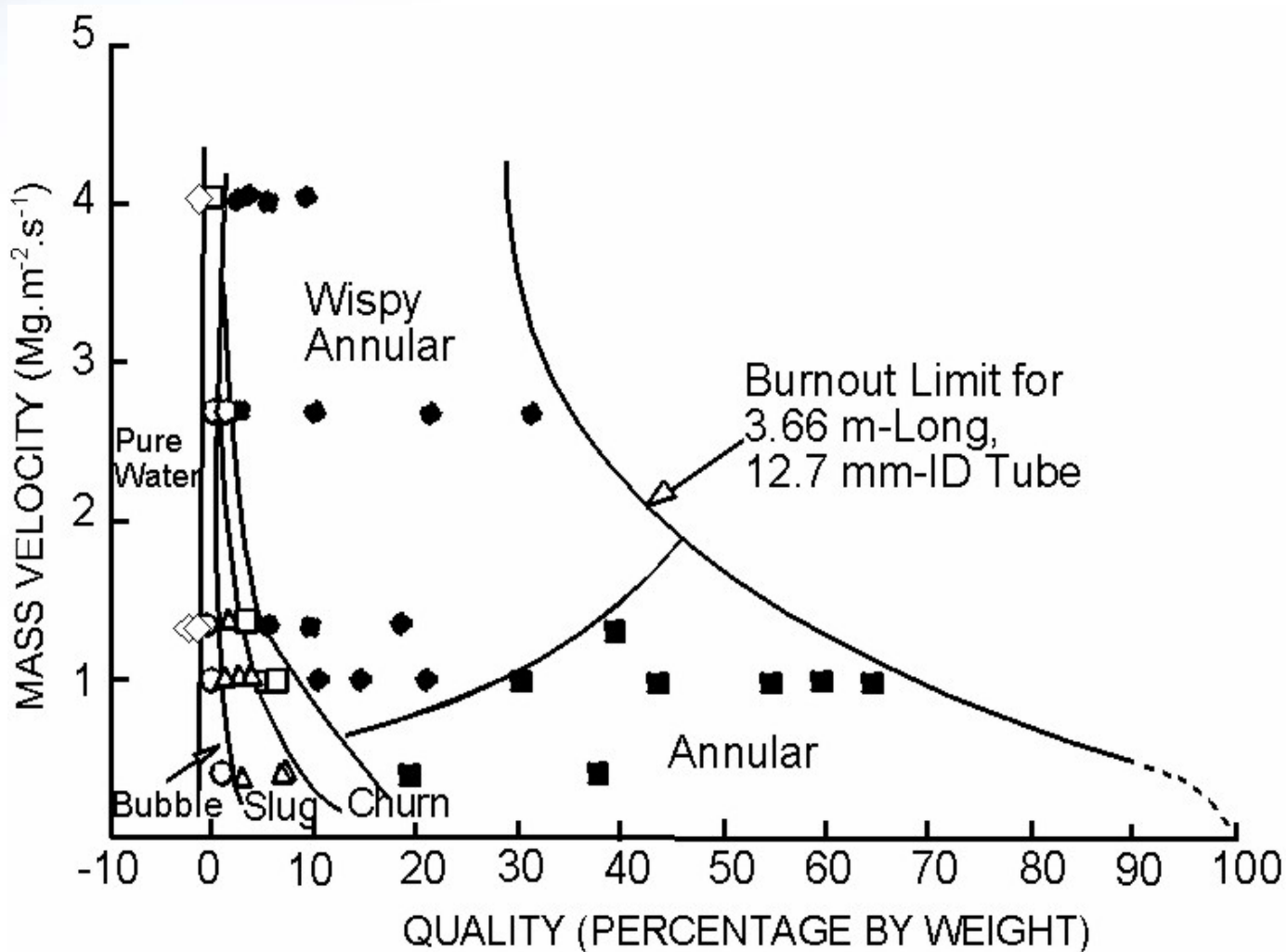


Flow Patterns in Horizontal Heated Channel





Flow Pattern Map in a Heated Channel



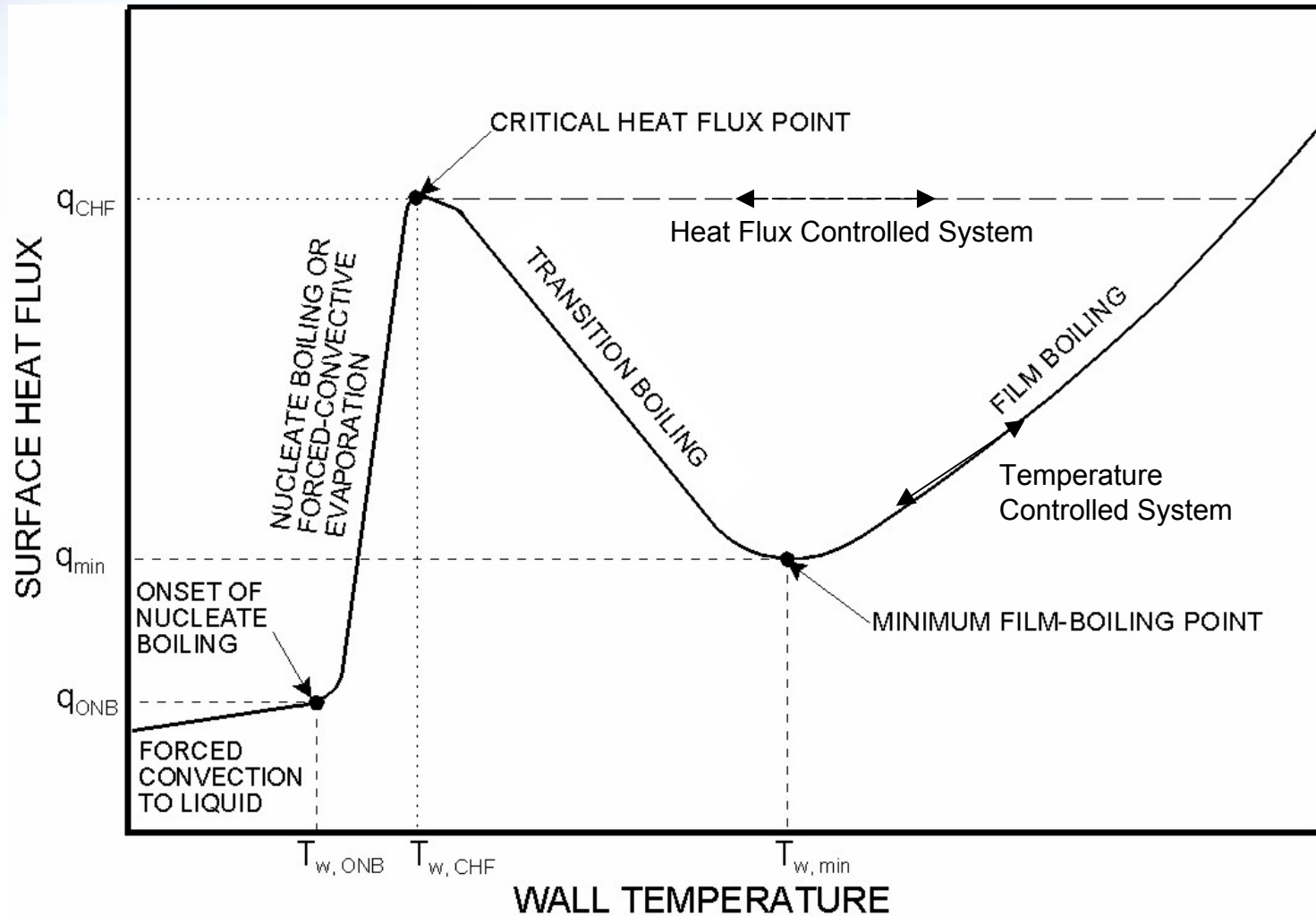


Definitions for Transition Points

- **Onset of nucleate boiling**
 - Transition point between single-phase and boiling heat transfer
- **Onset of net vapour generation (or significant void)**
 - Transition point between single-phase and two-phase flow (mainly for pressure-drop calculations)
- **Saturation point**
 - Boiling initiation point in an equilibrium system
- **Critical heat flux point**
 - Transition point between nucleate boiling and transition/film boiling
- **Minimum film-boiling point**
 - Transition point between transition boiling and film boiling



Boiling Curve





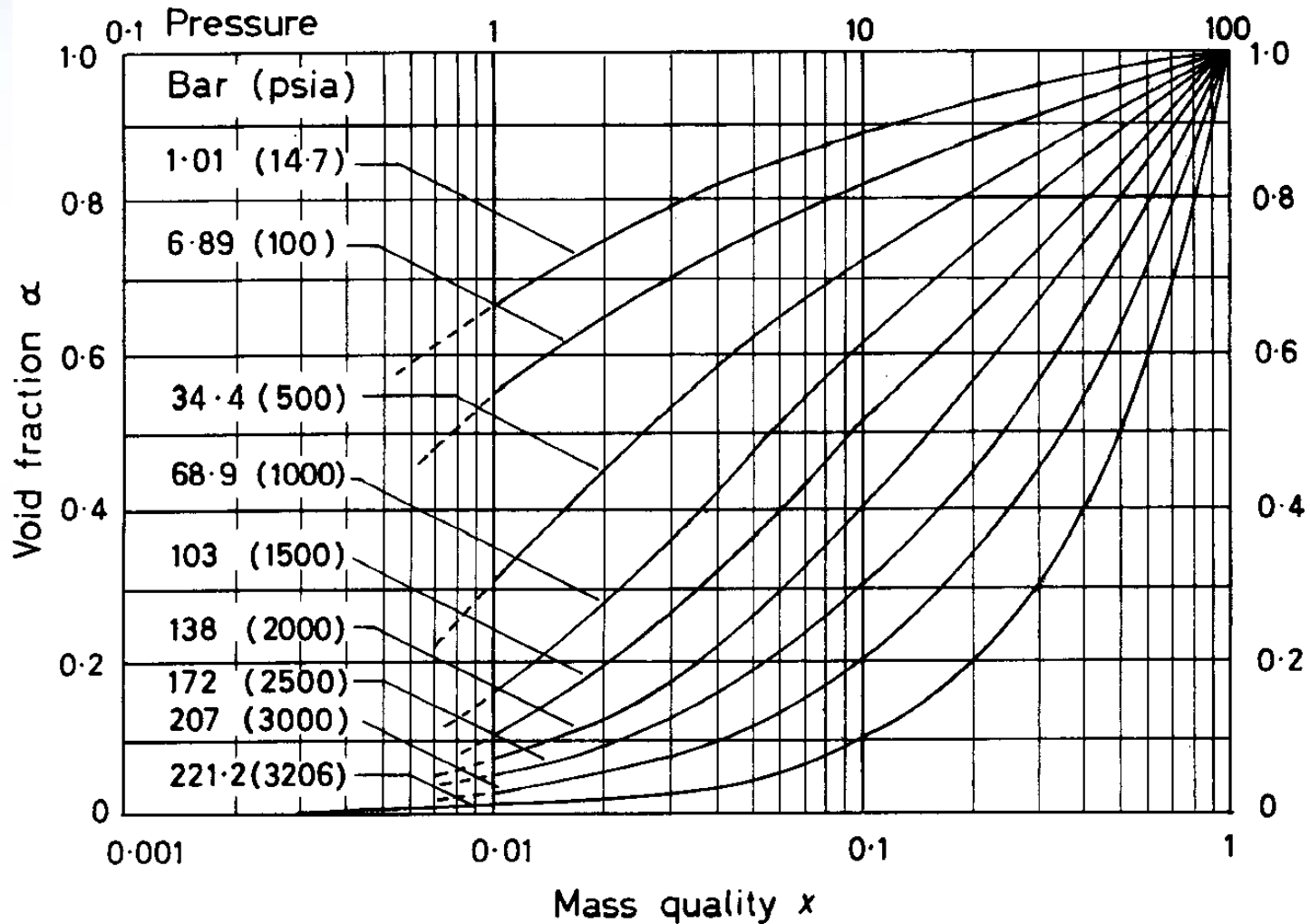
Void Fraction

- **Ratio of vapour flow area to total flow area**
- **Depends strongly on pressure, mass flux, and quality**
- **Applied to calculate the acceleration pressure drop in steady-state homogeneous code**
- **Large number of correlations proposed**
 - Homogeneous equation is the simplest
 - Chexal correlation is the most complex
 - Armand-Massina correlation is applied in the NUCIRC code
- **Solved from the conservation equations in two-fluid reactor safety codes**



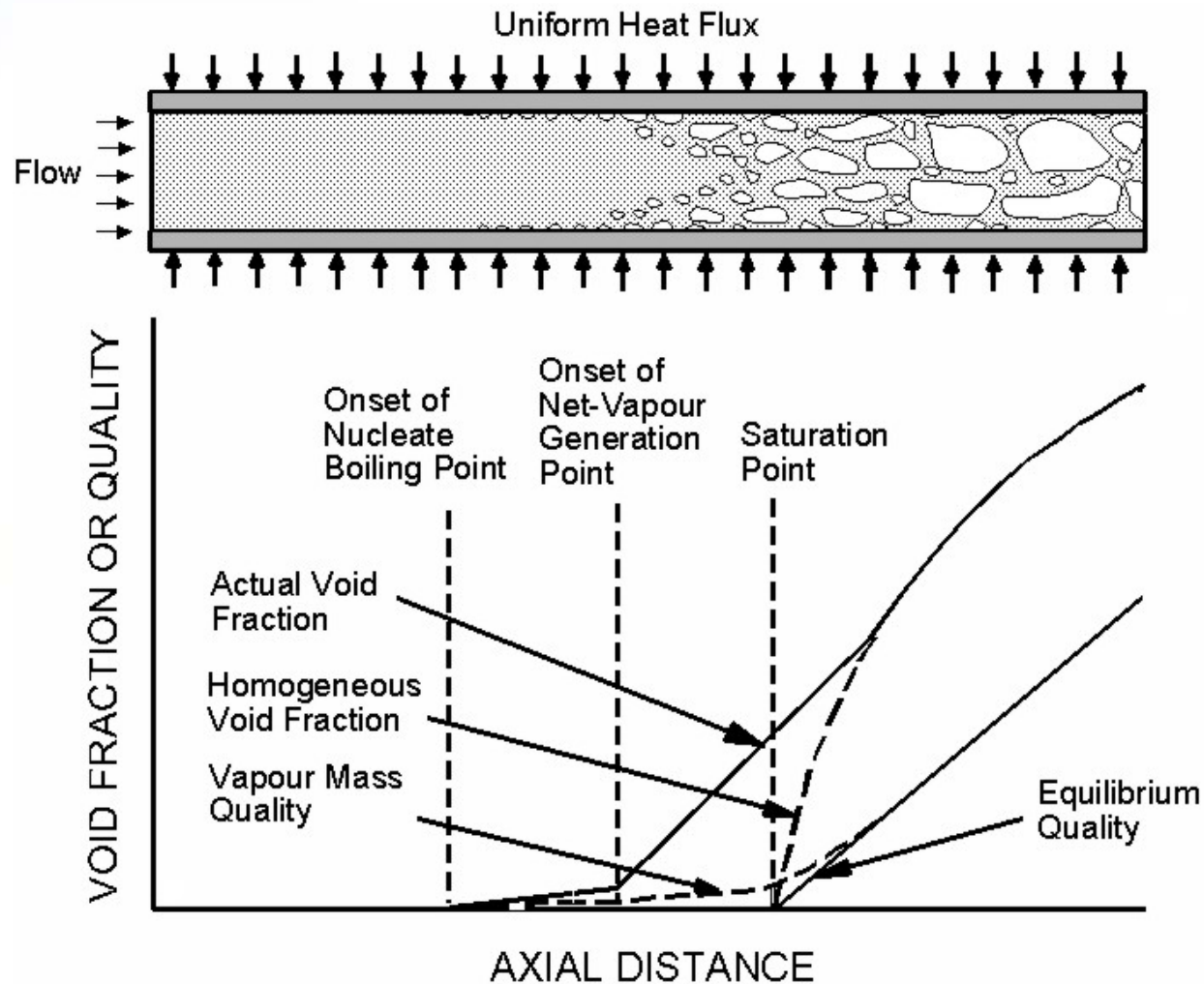
Effects of Pressure and Quality

Quality % by wt.



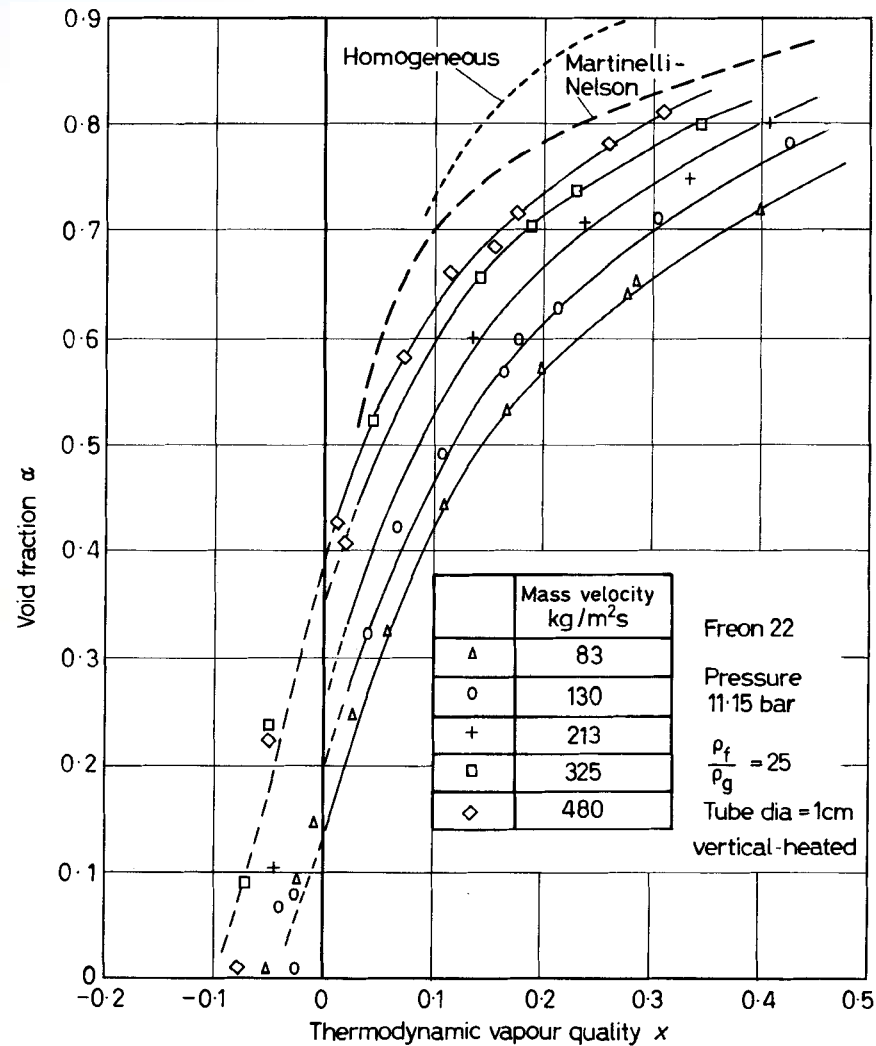


Subcooled Boiling





Subcooled Void Measurements





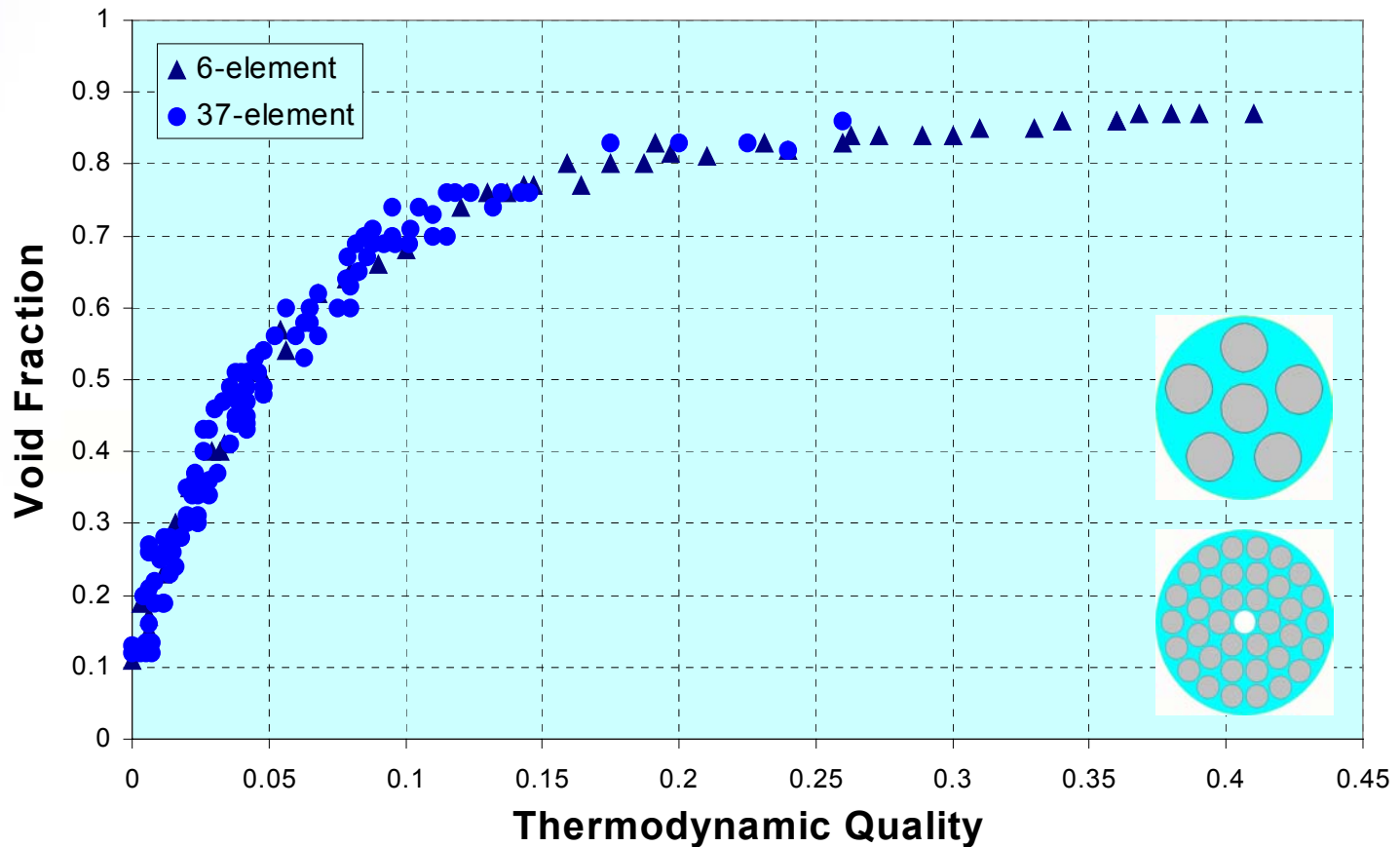
Void Fraction in Bundles

- **Void-fraction database**
 - Tube, annuli, and bundles (from 3 to 37 elements).
 - Covered a wide range of flow conditions.
 - Uniformly heated (axial and radial)
 - A bundle in various sizes of flow tube.
- **Effect of bundle geometry on void fraction is small.**
- **Effect of mass flux is strong.**
- **Changes in flow-tube size and heat flux affect mainly the low-quality region (change in onset of significant void).**



Bundle Geometry Effect

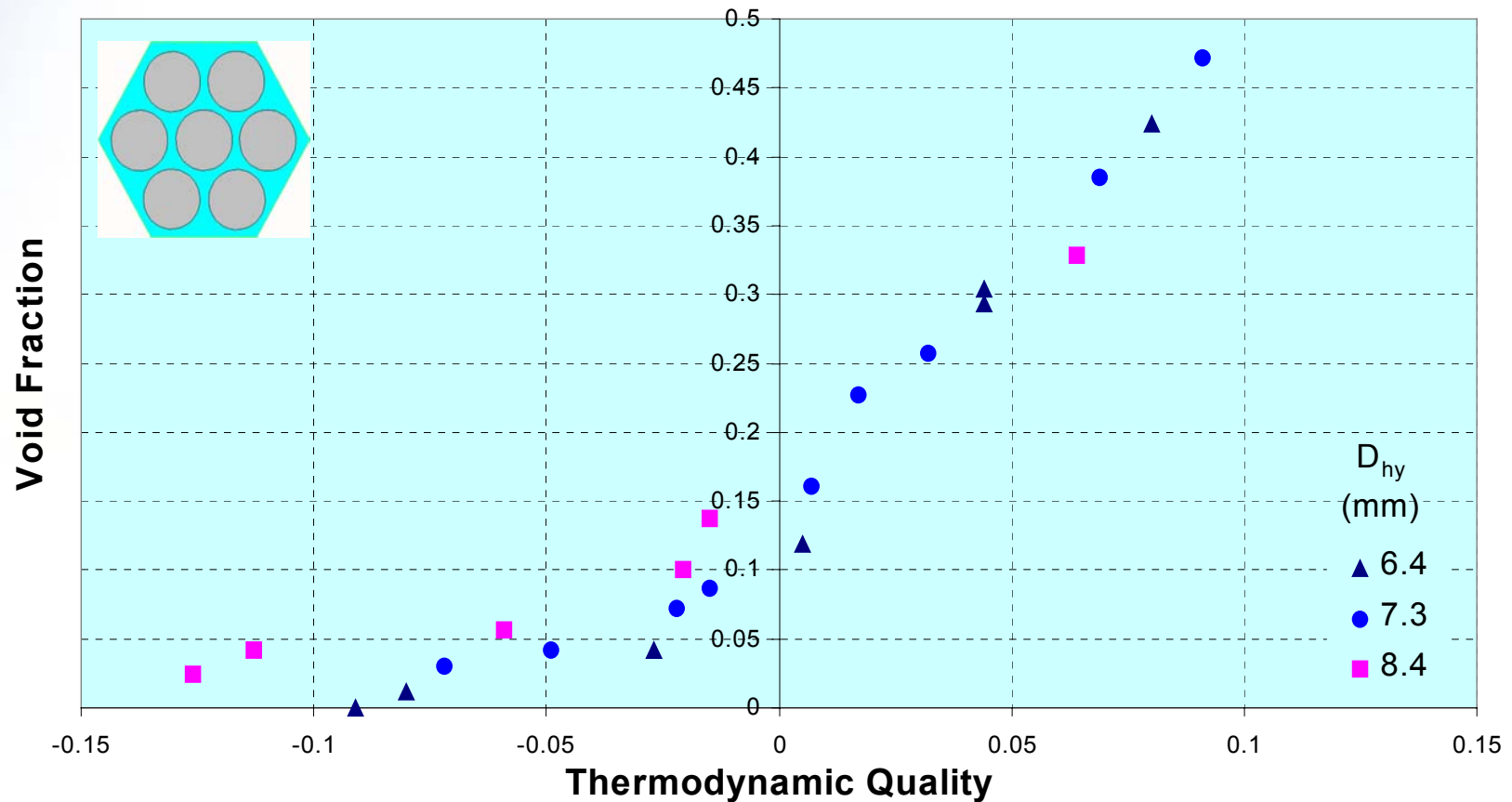
Pressure: 5 MPa, Mass Flux: 0.5 to 1.6 $\text{Mg}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$,
Heat Flux: 0.1 to 0.98 $\text{MW}\cdot\text{m}^{-2}$





Effect of Flow Tube Size

Pressure: 9.8 MPa, Mass Flux: 2 Mg.m⁻².s⁻¹, Heat Flux: 0.8 MW.m⁻²





Void Fraction Correlations

- **Homogeneous equation**

$$\alpha = \frac{x_a v_g}{(1 - x_a) v_f + x_a v_g}$$

- **Armand-Massina correlation**

$$\alpha = \frac{(0.833 + 0.167 x_a) x_a v_g}{(1 - x_a) v_f + x_a v_g}$$



Specific Applications

- **Critical Flow**
- **Pump operation**
- **Natural Circulation (thermosyphoning)**



Summary

- **Two-phase flow terminologies and definitions presented**
- **Homogeneous and separated-flow models assumptions described**
- **Flow patterns and transition boundaries presented for vertical and horizontal flows in unheated and heated tubes**
- **Convective boiling and heat-transfer modes described**
- **Void fraction data and correlations illustrated**



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